



## Cube Roots (page 1)

A **cube root** of a number is a number that, when multiplied by itself, and the multiplied by itself again, equals the given number. A **perfect cube** is a number with an integer as its cube root. The symbol used for a cube root:  $\sqrt[3]{\quad}$ .

**Examples:** Find the cube roots:

a)  $\sqrt[3]{8} = 2$  because  $2 \cdot 2 \cdot 2 = 2^3$ ,  $2^3 = 8$ , so  $\sqrt[3]{8} = \sqrt[3]{2^3} = 2$

b)  $\sqrt[3]{-27} = -3$  because  $-3(-3)(-3) = (-3)^3$ ,  $(-3)^3 = -27$ , so  $\sqrt[3]{-27} = \sqrt[3]{(-3)^3} = -3$

c)  $\sqrt[3]{\frac{8}{27}} = \frac{2}{3}$

Evaluate the expressions:

a)  $4\sqrt[3]{27} = 4(3)$   
 $= 12$

b)  $(\sqrt[3]{64})^3 + 8 = 64 + 8$   
 $= 72$

c)  $\sqrt[3]{-\frac{27}{64}} = -\frac{3}{4}$

d)  $\sqrt[3]{1} = 1$

e)  $\sqrt[3]{-216} = -6$

f)  $17 - 2\sqrt[3]{8} = 17 - 2(2)$   
 $= 13$

Solve for  $x$ .

a)  $x^3 = 125$

$$\begin{aligned} x^3 &= 125 \\ \sqrt[3]{x^3} &= \sqrt[3]{125} \\ x &= 5 \end{aligned}$$

b)  $x^3 = -64$

$$\begin{aligned} x^3 &= -64 \\ \sqrt[3]{x^3} &= \sqrt[3]{-64} \\ x &= -4 \end{aligned}$$

- c) Using the formula for volume of a cube,  $V = s^3$ , find the edge length for a cube with a volume of  $27 \text{ in}^3$ .

$$\begin{aligned} V &= s^3 \\ 27 &= s^3 \\ \sqrt[3]{27} &= \sqrt[3]{s^3} \\ 3 &= s \end{aligned}$$

The edge length is 3 inches.

## Cube Roots (page 2)

*Find the value of each perfect cube:*

1.  $3^3$

2.  $5^3$

3.  $10^3$

4.  $1^3$

5.  $7^3$

6.  $20^3$

*Find the cube root of the number:*

7. 27

8. 64

9. 1000

10. 729

*Simplify the expressions:*

11.  $3\sqrt[3]{8}$

12.  $(\sqrt[3]{64})^3 + 27$

13.  $\sqrt[3]{-\frac{64}{125}}$

14.  $\sqrt[3]{-1}$

15.  $\sqrt[3]{343}$

16.  $20 - 4\sqrt[3]{8}$

*Solve:*

17.  $x^3 = 8$

18.  $x^3 = 216$

19.  $x^3 = -27$

20.  $x^3 = 343$

21.  $x^3 = -729$

22.  $x^3 = 1$

23. The volume of a Rubik's cube is  $216 \text{ cm}^3$ , what is the length of one of its sides?