



Cube Roots (page 1)

A **cube root** of a number is a number that, when multiplied by itself, and the multiplied by itself again, equals the given number. A **perfect cube** is a number with an integer as its cube root. The symbol used for a cube root: $\sqrt[3]{\quad}$.

Examples: Find the cube roots:

a) $\sqrt[3]{8} = 2$ because $2 \cdot 2 \cdot 2 = 2^3$, $2^3 = 8$, so $\sqrt[3]{8} = \sqrt[3]{2^3} = 2$

b) $\sqrt[3]{-27} = -3$ because $-3(-3)(-3) = (-3)^3$, $(-3)^3 = -27$, so $\sqrt[3]{-27} = \sqrt[3]{(-3)^3} = -3$

c) $\sqrt[3]{\frac{8}{27}} = \frac{2}{3}$

Evaluate the expressions:

a) $4\sqrt[3]{27} = 4(3)$
 $= 12$

b) $(\sqrt[3]{64})^3 + 8 = 64 + 8$
 $= 72$

c) $\sqrt[3]{-\frac{27}{64}} = -\frac{3}{4}$

d) $\sqrt[3]{1} = 1$

e) $\sqrt[3]{-216} = -6$

f) $17 - 2\sqrt[3]{8} = 17 - 2(2)$
 $= 13$

Solve for x .

a) $x^3 = 125$

$$\begin{aligned} x^3 &= 125 \\ \sqrt[3]{x^3} &= \sqrt[3]{125} \\ x &= 5 \end{aligned}$$

b) $x^3 = -64$

$$\begin{aligned} x^3 &= -64 \\ \sqrt[3]{x^3} &= \sqrt[3]{-64} \\ x &= -4 \end{aligned}$$

- c) Using the formula for volume of a cube, $V = s^3$, find the edge length for a cube with a volume of 27 in^3 .

$$\begin{aligned} V &= s^3 \\ 27 &= s^3 \\ \sqrt[3]{27} &= \sqrt[3]{s^3} \\ 3 &= s \end{aligned}$$

The edge length is 3 inches.

Cube Roots (page 2)

Find the value of each perfect cube:

1. 3^3

2. 5^3

3. 10^3

4. 1^3

5. 7^3

6. 20^3

Find the cube root of the number:

7. 27

8. 64

9. 1000

10. 729

Simplify the expressions:

11. $3\sqrt[3]{8}$

12. $(\sqrt[3]{64})^3 + 27$

13. $\sqrt[3]{-\frac{64}{125}}$

14. $\sqrt[3]{-1}$

15. $\sqrt[3]{343}$

16. $20 - 4\sqrt[3]{8}$

Solve:

17. $x^3 = 8$

18. $x^3 = 216$

19. $x^3 = -27$

20. $x^3 = 343$

21. $x^3 = -729$

22. $x^3 = 1$

23. The volume of a Rubik's cube is 216 cm^3 , what is the length of one of its sides?