



Lesson 4: Creating a Histogram

Student Outcomes

- Students construct a frequency histogram.
- Students recognize that the number of intervals may affect the shape of a histogram.

Classwork

This lesson organizes the development of the student outcomes in three examples. Example 1 introduces frequency tables with intervals. Example 2 discusses how to create a histogram from the data that is organized in the interval frequency table from Example 1. Example 3 discusses another feature of a histogram – its shape. Students are introduced to a mound/symmetric shape and a skewed shape. Following each example is an exercise set designed for independent or small group work to reinforce the main objectives of constructing and interpreting a histogram. Teacher selection of problems is encouraged. If all problems are completed, this lesson may take longer than one class period.

Example 1 (10 minutes): Frequency Table with Intervals

Example 1: Frequency Table with Intervals

The boys and girls basketball teams at Roosevelt Middle School wanted to raise money to help buy new uniforms. They decided to sell hats with the school logo on the front to family members and other interested fans. To obtain the correct hat size, the students had to measure the head circumference (distance around the head) of the adults who wanted to order a hat. The following data represents the head circumferences, in millimeters (mm), of the adults:

513, 525, 531, 533, 535, 535, 542, 543, 546, 549, 551, 552, 552, 553, 554, 555, 560, 561, 563, 563, 565,
565, 568, 568, 571, 571, 574, 577, 580, 583, 583, 584, 585, 591, 595, 598, 603, 612, 618

The hats come in six sizes: XS, S, M, L, XL, and XXL. Each hat size covers a span of head circumferences. The hat manufacturer gave the students the table below that shows the interval of head circumferences for each hat size. The interval $510 < 530$ represents head circumferences from 510 to 530, not including 530.

Hat Sizes	Interval of Head Circumferences (mm)	Tally	Frequency
XS	$510 < 530$		
S	$530 < 550$		
M	$550 < 570$		
L	$570 < 590$		
XL	$590 < 610$		
XXL	$610 < 630$		

This example begins with data from the GAISE (Guidelines for Assessment and Instruction in Statistics Education) Report published by the American Statistical Association (<http://www.amstat.org/education/gaise/index.cfm>). The example presents the data in a frequency table, but the head circumferences are grouped into intervals. You may want to display a frequency table from Lesson 3 and discuss with the students the similarities and differences. It is also important that students understand that each interval should be the same width and that they should not skip intervals even if there is no data for an interval.

MP.1 As students complete the following exercises, pose the following questions:

- How is the frequency table with intervals similar to the frequency tables from Lesson 3? How is it different?
- What is the span or width of each interval? Are all the intervals the same width?
- What patterns do you see in the interval column?

Exercises 1–4 (10 minutes)

The four exercises that follow are designed to help students understand the idea of grouping data in intervals.

Exercises 1–4

1. If someone has a head circumference of 570, what size hat would they need?
Large
2. Complete the tally and frequency columns in the table to determine the number of each size hat the students need to order for the adults who wanted to order a hat.

Hat Sizes	Interval of Head Circumferences (mm)	Tally	Frequency
XS	510–< 530		2
S	530–< 550	+++	8
M	550–< 570	+++ +++ +++	15
L	570–< 590	+++	9
XL	590–< 610		4
XXL	610–< 630		2
3. What hat size does the data center around?
Medium
4. Describe any patterns that you observe in the frequency column?
The numbers start small but increase to 15 and then go back down.

Example 2 (15 minutes): Histogram

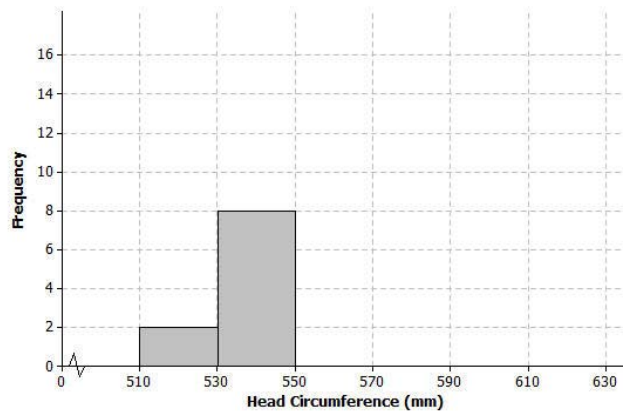
Example 2: Histogram

One student looked at the tally column and said that it looked somewhat like a bar graph turned on its side. A histogram is a graph that is like a bar graph, except that the horizontal axis is a number line that is marked off in equal intervals.

To make a histogram:

- Draw a horizontal line and mark the intervals.
- Draw a vertical line and label it “frequency.”
- Mark the frequency axis with a scale that starts at 0 and goes up to something that is greater than the largest frequency in the frequency table.
- For each interval, draw a bar over that interval that has a height equal to the frequency for that interval.

The first two bars of the histogram have been drawn below.



The students are introduced to a histogram in this example. They use the data that was organized in a frequency table with intervals in Example 1. You may want to begin this lesson by showing the students an example of a bar graph. For example, show a bar graph showing favorite pizza toppings. Point out the horizontal axis is *not* a number line, but contains categories. The vertical axis is the frequency (or count) of how many people chose the particular pizza topping. As you present the histogram to the students, point out the main difference is the horizontal axis is a number line, and the intervals are listed in order from smallest to largest. Some students may struggle with the notation for the intervals. Point out to the students that the interval labeled $510 < 530$, represents any head circumference from 510 mm to 530, not including 530. A head circumference of 530 is counted in the bar from $530 - 550$ and not in the bar from $510 - 530$.

Pose the following questions as students develop the following exercise:

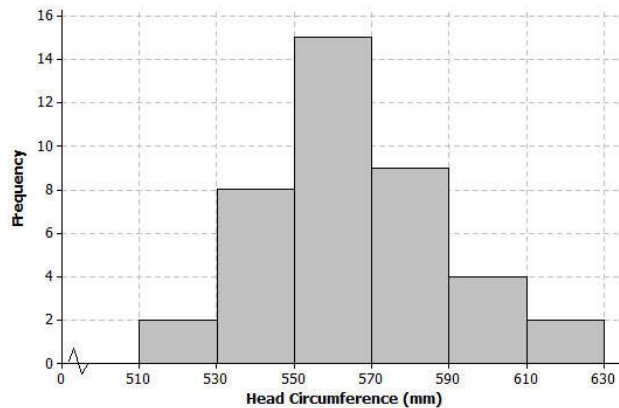
- Why should the bars touch each other in the histogram?
- How are histograms and bar graphs similar? How are they different?

Exercises 5–9 (10 minutes)

In the first problem, students are asked to complete the histogram. Emphasize that the bars should touch each other and be the same width. Also point out the jagged line (or “scissor cut”), and explain that it is used to indicate a cutting of the horizontal axis. (A “scissor cut” could also be used on a vertical axis.) The cut is used to show the graph by “pulling in” unused space.

Exercises 5–9

5. Complete the histogram by drawing bars whose heights are the frequencies for those intervals.



6. Based on the histogram, describe the center of the head circumferences.

Around 560 mm.

7. How would the histogram change if you added head circumferences of 551 and 569?

The bar in the 550 to 570 interval would go up to 17.

8. Because the 40 head circumference values were given, you could have constructed a dot plot to display the head circumference data. What information is lost when a histogram is used to represent a data distribution instead of a dot plot?

In a dot plot, you can see individual values. In a histogram, you only see the total number of values in an interval.

9. Suppose that there had been 200 head circumference measurements in the data set. Explain why you might prefer to summarize this data set using a histogram rather than a dot plot.

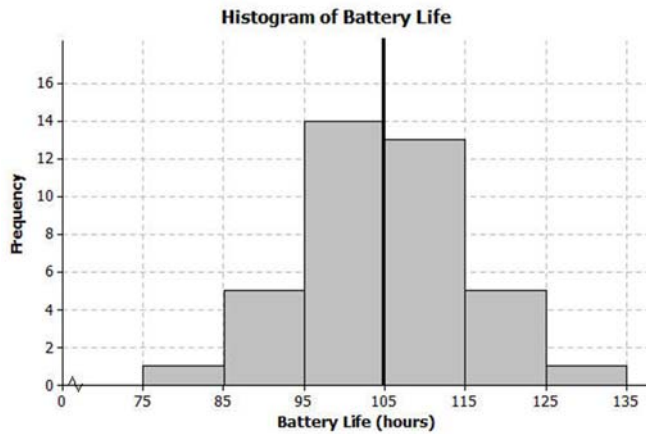
There would be too many dots on a dot plot, and it would be hard to read. A histogram would work for a large data set because the scale can be adjusted.

Example 3 (10 minutes): Shape of the Histogram

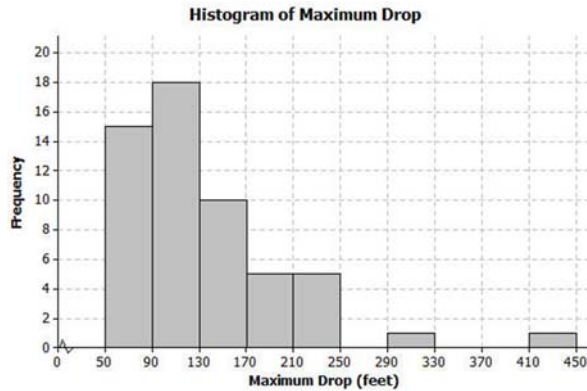
Example 3: Shape of the Histogram

A histogram is useful to describe the shape of the data distribution. It is important to think about the shape of a data distribution because depending on the shape, there are different ways to describe important features of the distribution, such as center and variability.

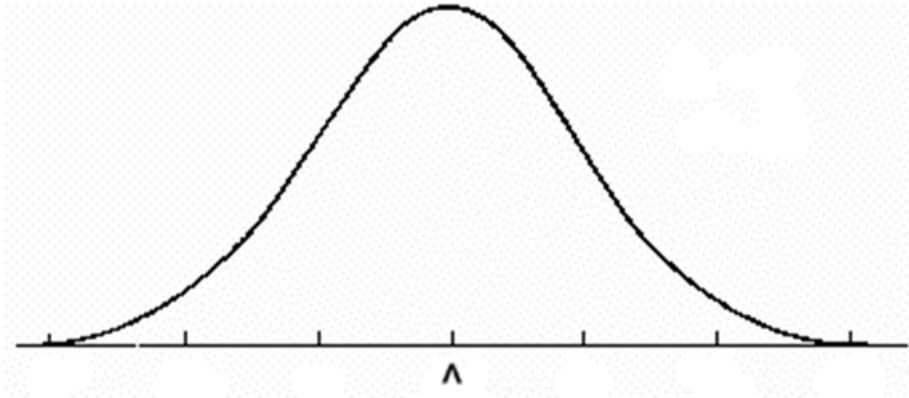
A group of students wanted to find out how long a certain brand of AA batteries lasted. The histogram below shows the data distribution for how long (in hours) that some AA batteries lasted. Looking at the shape of the histogram, notice how the data “mounds” up around a center of approximately 105. We would describe this shape as mound shaped or symmetric. If we were to draw a line down the center, notice how each side of the histogram is approximately the same or mirror images of each other. This means the graph is approximately symmetrical.



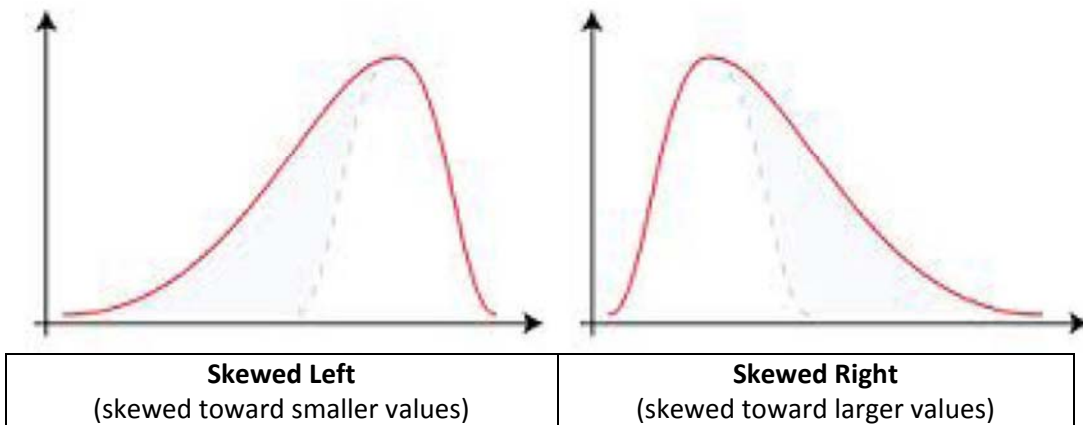
Another group of students wanted to investigate the maximum drop length for roller coasters. The histogram below shows the maximum drop (in feet) of a selected group of roller coasters. This histogram has a skewed shape. Most of the data are in the intervals from 50 to 170. But there are two values that are unusual (or not typical) when compared to the rest of the data. These values are much higher than most of the data.



MP.4 This example discusses the concept of the shape of a distribution and how it relates to center and variability. Two shapes are introduced, mound-shaped or symmetric and skewed. Below is an example of a symmetric (i.e., mound-shaped) distribution. The emphasis is on the approximate symmetry in the histogram.



Below are two examples of skewed distributions:



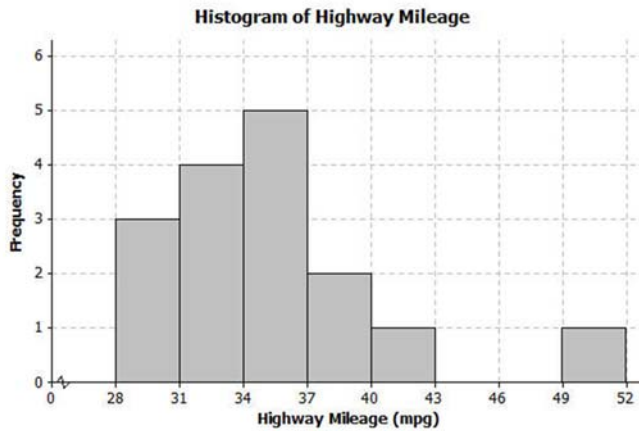
Point out to the students that a skewed distribution has values that are not typical of the rest of the data. They either could be data much greater than the rest of the data or much lower than the rest of the data. The graph will have a tail that is longer on one side than the other.

Exercises 10–12 (10 minutes)

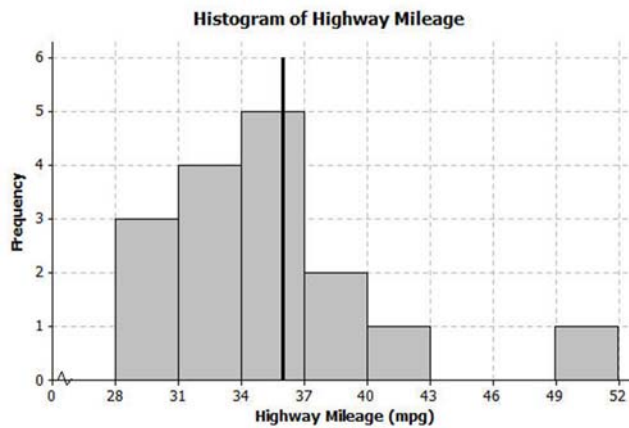
The next three questions are designed to help students classify a distribution as approximately symmetric (i.e., mound-shaped) or skewed.

Exercises 10–12

10. The histogram below shows the highway miles per gallon of different compact cars.



- a. Describe the shape of the histogram as approximately symmetric, skewed left, or skewed right.
Skewed right toward the larger values.
- b. Draw a vertical line on the histogram to show where the “typical” number of miles per gallon for a compact car would be.
Around 36.

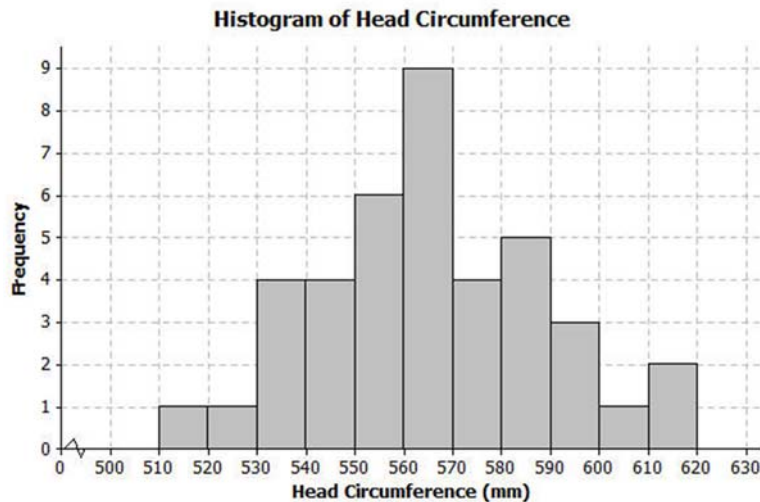


- c. What does the shape of the histogram tell you about miles per gallon for compact cars?
Most cars get around 31 to 40 mpg. But there was one car that got between 49 and 52 mpg.

11. Describe the shape of the head circumference histogram that you completed in Exercise 5 as approximately symmetric, skewed left, or skewed right.

Approximately symmetric.

12. Another student decided to organize the head circumference data by changing the width of each interval to be 10 instead of 20. Below is the histogram that the student made.



- a. How does this histogram compare with the histogram of the head circumferences that you completed in Exercise 5?

Answers will vary; same shape and center, but not as symmetric.

- b. Describe the shape of this new histogram as approximately symmetric, skewed left, or skewed right.

Approximately symmetric.

- c. How many head circumferences are in the interval from 570 to 590?

9

- d. In what interval would a head circumference of 571 be included? In what interval would a head circumference of 610 be included?

571 is in the interval from 570 to 580; 610 is in the interval from 610 to 620.

Lesson Summary

A histogram is a graph that represents the number of data values falling in an interval with a bar. The horizontal axis shows the intervals and the vertical axis shows the frequencies (how many data values are in the interval). Each interval should be the same width and the bars should touch each other.

Exit Ticket (7–10 minutes)

Name _____

Date _____

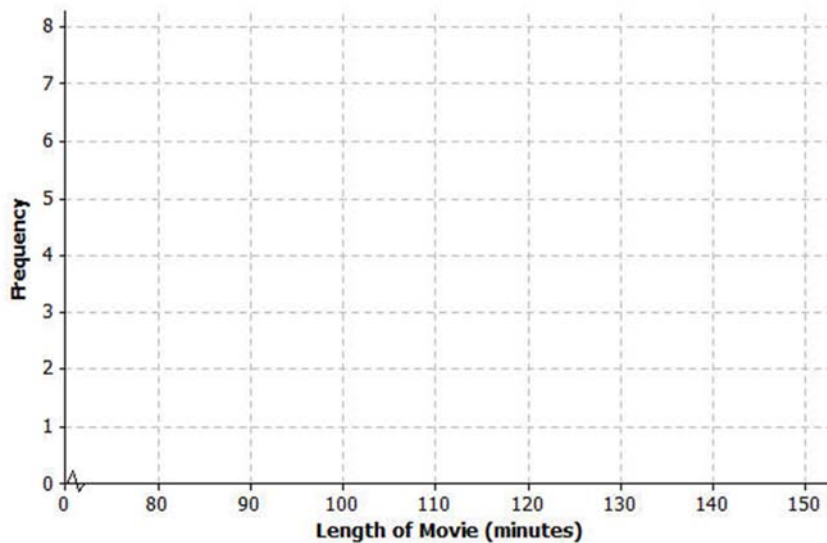
Lesson 4: Creating a Histogram

Exit Ticket

The frequency table below shows the length of selected movies shown in a local theater over the past six months.

Length of Movie (min)	Tally	Frequency
80–< 90		1
90–< 100		4
100–< 110	++++	7
110–< 120	+++	5
120–< 130	++++	7
130–< 140		3
140–< 150		1

- Construct a histogram for the length of movies data.



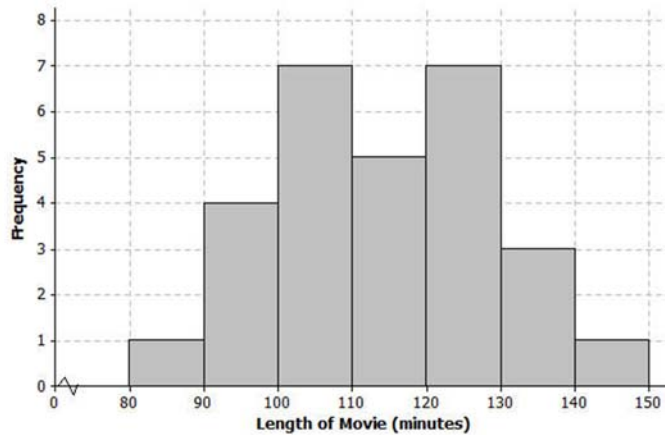
- Describe the shape of the histogram.
- What does the shape tell you about the length of movies?

Exit Ticket Sample Solutions

The frequency table below shows the length of selected movies shown in a local theater over the past six months.

Length of Movie (min)	Tally	Frequency
80–< 90		1
90–< 100		4
100–< 110		7
110–< 120		5
120–< 130		7
130–< 140		3
140–< 150		1

- Construct a histogram for the length of movies data.

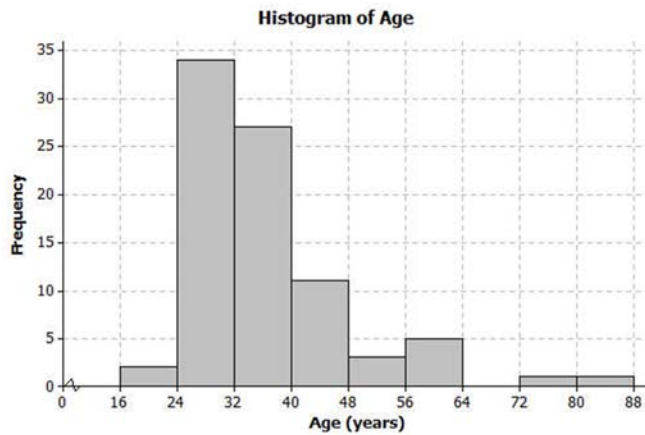


- Describe the shape of the histogram.
Mound shaped or approximately symmetric.
- What does the shape tell you about the length of movies?
Most movies lengths were between 100 and 130 minutes.

Problem Set Sample Solutions

Note that teacher discretion is encouraged for assigning problems from this problem set. Problems are provided to address the varying interests of students.

1. The following histogram shows ages of the actresses whose performances have won in the Best Leading Actress category at the annual Academy Awards (Oscars).

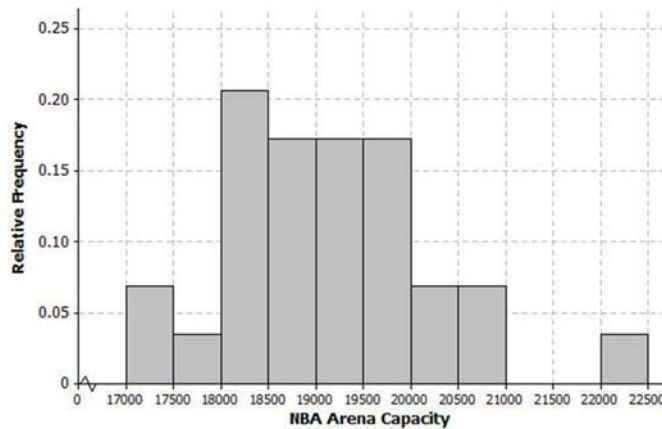


- a. Which age interval contains the most actresses? How many actresses are represented in that interval?
The interval 24 to 32 contains the most actresses. There are 34 actresses whose age falls into that category.
- b. Describe the shape of the histogram.
Skewed to the right.
- c. What does the shape tell you about the ages of actresses who win the Oscar for best actress award?
Most of the ages are between 24 and 40, with two ages much larger than the rest.
- d. Which interval describes the center of the ages of the actresses?
32 to 40
- e. An age of 72 would be included in which interval?
It is in the interval from 72 to 80.

2. The frequency table below shows the seating capacity of arenas for NBA basketball teams.

Number of seats	Tally	Frequency
17000–< 17500		2
17500–< 18000		1
18000–< 18500		6
18500–< 19000		5
19000–< 19500		5
19500–< 20000		5
20000–< 20500		2
20500–< 21000		2
21000–< 21500		0
21500–< 22000		0
22000–< 22500		1

a. Draw a histogram of the number of seats in NBA arenas. Use the histograms you have seen throughout this lesson to help you in the construction of your histogram.



b. What is the width of each interval? How do you know?

The width of each interval is 500.

Subtract the values identifying an interval.

c. Describe the shape of the histogram.

Skewed to the right.

d. Which interval describes the center of the number of seats?

19,000 to 19,500

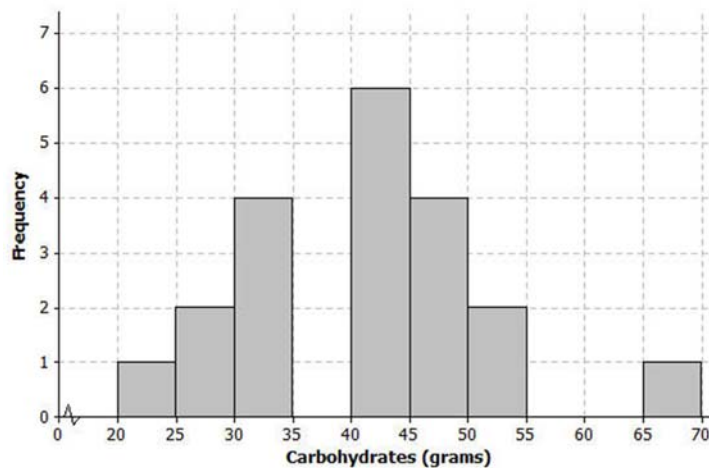
3. Listed are the grams of carbohydrates in hamburgers at selected fast food restaurants.

33 40 66 45 28 30 52 40 26 42
42 44 33 44 45 32 45 45 52 24

a. Complete the frequency table with intervals of width 5.

Number of carbohydrates (grams)	Tally	Frequency
20–< 25		1
25–< 30		2
30–< 35		4
35–< 40		0
40–< 45		6
45–< 50		4
50–< 55		2
55–< 60		0
60–< 65		0
65–< 70		1

b. Draw a histogram of the carbohydrate data.



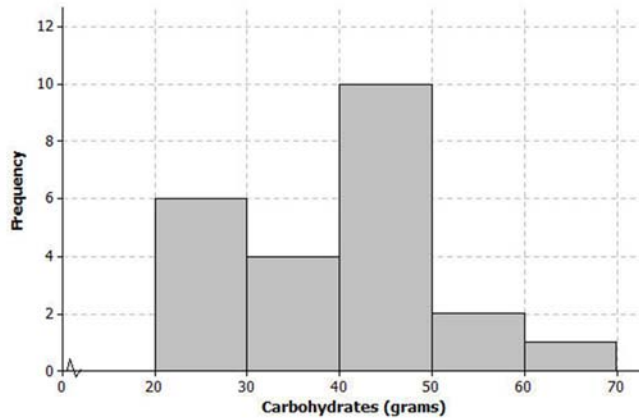
c. Describe the center and shape of the histogram.

Center is around 40; it is mound shaped.

d. In the frequency table below, the intervals are changed. Using the carbohydrate data above, complete the frequency table with intervals of width 10.

Number of carbohydrates (grams)	Tally	Frequency
20–< 30		3
30–< 40		4
40–< 50	+	10
50–< 60		2
60–< 70		1

- e. Draw a histogram.



4. Use the histograms that you constructed in question 3 parts (b) and (e) to answer the following questions.

- a. Why are there fewer bars in the histogram in question 3 part (e) than the histogram in part (b)?

There are fewer bars because the width of the interval changed from 5 grams to 10 grams, so there are fewer intervals.

- b. Did the shape of the histogram in question 3 part (e) change from the shape of the histogram in part (b)?

Generally, both are mound shaped, but the histogram in question 3 part (b) has gaps.

- c. Did your estimate of the center change from the histogram in question 3 part (b) to the histogram in part (e)?

The centers of the two histograms are about the same.