Lesson 4: Efficiently Adding Integers and Other Rational

Numbers

Student Outcomes

- Students understand the rules for adding integers:
 - Add integers with the same sign by adding the absolute values and using the common sign.
 - Add integers with opposite signs by subtracting the smaller absolute value from the larger absolute value and using the sign of the number with the larger absolute value.
- Students justify the rules using arrows and a number line or by using the Integer Game and extend their findings to begin to include sums of rational numbers.

Classwork

Exercise 1 (6 minutes): Hands Up, Pair Up!

MP.

Students review concepts from Lessons 1 through 3 by playing the Kagan Strategy Game, "Hands Up, Pair Up!" (Refer to the description at the end of this lesson.)¹ During play, students should critique each other's questions when necessary. They should use accurate vocabulary learned so far in this module when explaining and defending their answers. The following are possible student questions:

- When playing the Integer Game, you have cards in your hand with a sum of Then, you draw a card. Using addition, how would you write an equation to represent your score?
- What is the absolute value of ?
- What is the sum of
- In what direction does the arrow point on a number line for a negative number?
- What is an additive inverse of ? What is the additive inverse of ? What is the additive inverse of a number?

¹ Allow students 1-2 minutes for students to think of a question and record it on an index card. Write the answer to the question on the back. Ask the class to stand up, each person with one hand in the air. Students will find partners and greet each other with a high-five. Once a pair is formed, partners will take turns asking each other their questions. After both partners have asked and answered each other's questions, they will switch cards. Both partners will again raise their hands to signify they are ready for a new partner and repeat the activity. Allow enough time for each student to partner with 2-3 different people.



Efficiently Adding Integers and Other Rational Numbers 4/8/14



Scaffolding:

- Provide some pre-made index cards for learners who struggle forming a question with limited time.
- Ask students to refer to anchor posters for support during the game.



This work is licensed under a Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License



Example 1 (5 minutes): Rule for Adding Integers with Same Signs

The teacher leads the whole class to find the sum of . In the Integer Game, I would combine and to give me .





Lesson 4: Date:

Efficiently Adding Integers and Other Rational Numbers 4/8/14

(cc) BY-NC-SA





The teacher writes the rule for adding integers with the same sign.

RULE: Add integers with the same sign by adding the absolute values and using the common sign.



Lesson 4: Date:

Efficiently Adding Integers and Other Rational Numbers 4/8/14







Exercise 2 (5 minutes)

Students work in pairs while solving practice problems.





Lesson 4:

Efficiently Adding Integers and Other Rational Numbers 4/8/14





Example 2 (8 minutes): Rule for Adding Opposite Signs

The teacher leads the whole class to find the sum of . In the Integer Game, I would combine and to give me .





Lesson 4: Date: Efficiently Adding Integers and Other Rational Numbers 4/8/14

engage^{ny}



This work is licensed under a <u>Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.</u> iii. Write a rule that will give the length and direction of the arrow representing the sum of two values that have opposite signs. The length of the arrow of the sum is the difference of the value and value, or the two addends. The

direction of the arrow of the sum is the same as the direction of the longer arrow.

The teacher writes the rule for adding integers with opposite signs.

RULE: Add integers with opposite signs by subtracting the absolute values and using the sign of the integer with the greater absolute value.

Exercise 3 (5 minutes)

Students work in pairs practicing addition with opposite signs. The teacher will monitor student work and provide support when necessary.

Exercise 3					
1.	Circle the integer with the greater absolute value. Decide whether the sum will be positive or negative without actually calculating the sum.				
	a.	<u>positive</u>			
	b.	<u>negative</u>			
	c.	<u>negative</u>			
	d.	<u>negative</u>			
2.	Find the following sums	5:			
	a.				
	b.				
	с.				
	d.				



Lesson 4:

Efficiently Adding Integers and Other Rational Numbers 4/8/14



Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.



This work is licensed under a



Example 3 (5 minutes): Applying Integer Addition Rules to Rational Numbers

The teacher will pose the example to the whole class. Students will follow along in their student materials. The teacher will pose additional questions to the class.

- Which addend has the greatest absolute value (length of the arrow)? What direction does this arrow point? .
 - (The arrow length for is units long and to the right.)
 - - (The arrow length for - is - units long and to the left.)
- What is the length of this arrow?
- What is the final sign? What is the direction of the resulting arrow?
 - Since 6 has the greater absolute value (arrow length), my answer will be positive, so

Example 3: Applying Integer Addition Rules to Rational Numbers		
Find the sum of — . The addition of rational numbers follows the same rules of addition for integers.		
a. Find the absolute values of the numbers.		
b. Subtract the absolute values.		
○		
c. The answer will take the sign of the number that has the greater absolute value.		
Since has the greater absolute value (arrow length), my answer will be positive —.		

Exercise 4 (5 minutes)

Students work independently while solving practice problems.

Exercise 4		
Solve the following problems. Show your work.		
a. Find the sum of .		



Lesson 4:

Efficiently Adding Integers and Other Rational Numbers 4/8/14







Closing (3 minutes)

The teacher calls on students at random to summarize the lesson.

- What are the rules of adding numbers with opposite signs?
- What is the sum of
- What do you think the rules would be for subtracting numbers with same sign? (Do not spend too much time on this question. Allow students to verbally experiment with their responses.)

?

- Scaffolding:
- To help build confidence, allow students time to "turn and talk" with partners before posing questions.

Lesson Summary

- Add integers with the same sign by adding the absolute values and using the common sign.
- Steps to adding integers with opposite signs:
 - 1. Find the absolute values of the integers.
 - 2. Subtract the absolute values.
 - 3. The answer will take the sign of the integer that has the greater absolute value.
- To add rational numbers, follow the same rules used to add integers.

Exit Ticket (5 minutes)



Lesson 4: Date: Efficiently Adding Integers and Other Rational Numbers 4/8/14





Name

Date

Lesson 4: Efficiently Adding Integers and Other Rational Numbers

Exit Ticket

- 1. Write an addition problem that has a sum of and
 - a. Both addends (-value and -value) have the same sign.

b. The two addends (-value and -value) have different signs.

2. In the Integer Game, what card would you need to draw to get a score of if you have a , , and in your hand?



Efficiently Adding Integers and Other Rational Numbers 4/8/14







Exit Ticket Sample Solutions

1.	Write an addition problem that has a sum of — and			
	a.	Both addends (p-value and q-value) have the same sign.		
		Answers will vary. – –.		
	b.	The two addends (-value and -value) have different signs. Answers will vary.		
2.	In th hand	e Integer Game, what card would you need to draw to get a score of if you have a ?	and	in your
		, so I would need to draw a because is the additive inverse of .	•	

Problem Set Sample Solutions

Students must understand the rules for addition of integers and other numbers with same and opposite signs. The problem set presents multiple representations of these rules including diagrams, equations, and story problems. Students are expected to show their work or provide an explanation where necessary to justify their answers. Answers can be represented in fraction or decimal form.

1.	Find the sums. Show your work to justify your answer.						
	a.						
	ь. b.						
	c.						
	d.						
	e. — —						
2.	Which of these story problems describes the sum? Check all that apply. Show your work to justify your answer.						
	X Jared's dad paid him for raking the leaves from the yard on Wednesday. Jared spent at the movie theater on Friday. How much money does Jared have left?						
	Jared owed his brother for raking the leaves while Jared was sick. Jared's dad gave him for doing his chores for the week. How much money does Jared have now?						
	<u>X</u> Jared's grandmother gave him for his birthday. He bought \$ worth of candy and spent another on a new comic book. How much money does Jared have left over?						



Lesson 4:

Efficiently Adding Integers and Other Rational Numbers 4/8/14









COMMON Le CORE D

Lesson 4: Date: Efficiently Adding Integers and Other Rational Numbers 4/8/14

