Special Functions



Name______Period_____Date____

NON-CALCULATOR SECTION

Vocabulary: Define each word and give an example.

- 1. Step Function
- 2. Domain

Short Answer:

- 3. How is an absolute value function a piecewise function?
- 4. How is the inverse of a function related to the function?

Review:

- 5. Solve by factoring: $2x^2 3x 5 = 0$
- 6. Solve: 3|x-5|+7=25
- 7. Solve the system: y = 2x + 53x y = -2

Problems:

Be sure to **show all work used to obtain your answer. Circle or box in the final answer.**

- 8. If f(3) = 7 and g is the inverse of f, then g(7) = ?
- 9. Find the inverse of the function: $\{(3,-2),(8,1),(0,0),(2,5),(-4,7)\}$



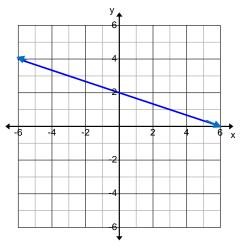
10. Find $f^{-1}(x)$ for the functions below. Show all work.

a.
$$f(x) = 2x - 5$$

a.
$$f(x) = 2x - 5$$
 b. $f(x) = -\frac{1}{2}x + 1$ c. $f(x) = \frac{3}{4}x - 6$

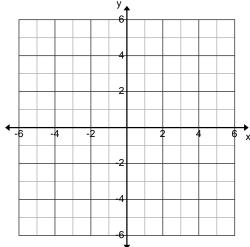
c.
$$f(x) = \frac{3}{4}x - 6$$

11. Graph the inverse of the given function:



12. Find the inverse of the function. Then, graph the original function and its inverse on the graph at the right.

$$f(x) = 4x - 6$$



- 13. Evaluate the following for $f(x) = \begin{cases} 2|x-1|, & x \le -1\\ 4x+3, & -1 < x < 2\\ 5, & x \ge 2 \end{cases}$

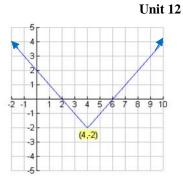
 - a. f(0) b. f(-1) c.
 - f(8)
- d. f(1)

Algebra I Practice Test

Special Functions



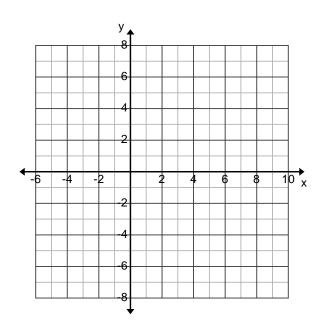
14. Write the equation for the graph shown at the right as a piece-wise defined function.

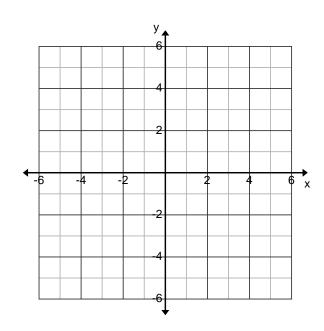


15. Graph the piecewise functions below:

a.
$$f(x) = \begin{cases} 2x-1, & x \le 2 \\ x-3, & x > 2 \end{cases}$$

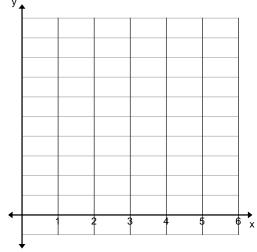
b.
$$f(x) = \begin{cases} x+1, & x \le -1 \\ 3, & -1 < x \le 2 \\ 2x-4, & x > 2 \end{cases}$$





16. An automotive repair center charges \$50 for any part of the first hour of labor and \$35 for any part of each additional hour. Fill in the table below where x is the number of hours of labor and T(x) is the total labor charge. Then, graph the function at the right.

X	T(x)
$0 < x \le 1$	
$1 < x \le 2$	
$2 < x \le 3$	
$3 < x \le 4$	
$4 < x \le 5$	

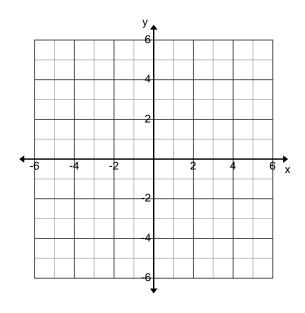


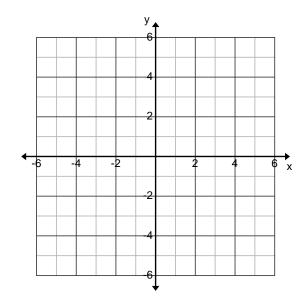


17. Graph the absolute value functions below.

a.
$$f(x) = |x-2|-4$$

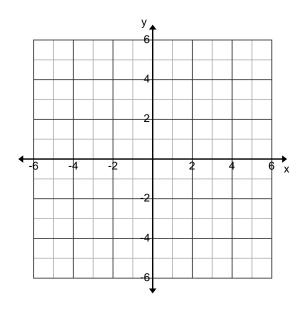
b.
$$y = -|x+2|+3$$

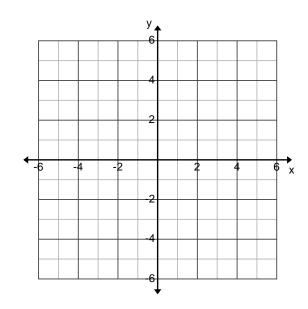




c.
$$y = 2|x+1|-1$$

$$d. y = \frac{1}{2} |x| - 4$$

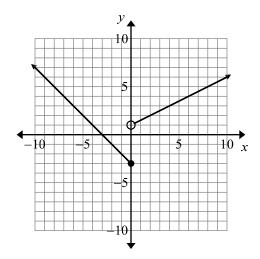






Multiple Choice Section: Circle the best answer.

18. Which function is represented by the graph?



A.
$$f(x) = \begin{cases} -x - 3, & \text{if } x \le 0 \\ \frac{1}{2}x + 1, & \text{if } x > 0 \end{cases}$$

B.
$$f(x) = \begin{cases} x-3, & \text{if } x \le 0 \\ -\frac{1}{2}x+1, & \text{if } x > 0 \end{cases}$$

c.
$$f(x) = \begin{cases} -x+3, & \text{if } x \le 0 \\ \frac{1}{2}x+1, & \text{if } x > 0 \end{cases}$$

D.
$$f(x) = \begin{cases} x+3, & \text{if } x \le 0 \\ -\frac{1}{2}x+1, & \text{if } x > 0 \end{cases}$$

19. A function f(x) takes values of x and applies the following:

Step 1) divide x by 5

Step 2) subtract 3 from the result in Step 1

Which of these describes the inverse function of f(x)?

- A. Step 1) multiply *x* by 5 Step 2) add 3 to the result in Step 1
- **B.** Step 1) subtract 3 from *x* Step 2) divide the result in Step 1 by 5
- C. Step 1) add 3 to x
 Step 2) multiply the result in Step 1 by 5
- **D.** Step 1) divide x by 1/5 Step 2) subtract -3 from the result in Step 1

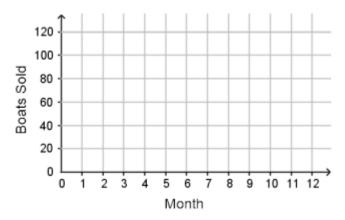


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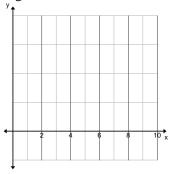
CALCULATOR SECTION

1. The number of boats, B, a boat dealer sells in each month of the year from March to December can be modeled by the function B = -15|t-5|+120, where t is the time in months and t = 1 represents January. Complete the table of values and then graph the function.

Time (months)	Boats Sold
3	
5	
7	
9	
11	
12	



- a. What is the maximum number of sales in one month? In what month is the maximum reached?
- b. What is the minimum number of sales in one month? In what month is the minimum reached?
- 2. During a nine hour snowstorm, it snows at a rate of 1 inch per hour for the first two hours, at a rate of 2 inches per hour for the next six hours, and at a rate of 1 inch per hour for the final hour.
 - a. Write and graph a piecewise function that gives the depth of the snow during the snowstorm.



- b. How many inches of snow accumulated from the storm?
- 3. The equation f(x) = 2.3x + 61 can be used to approximate height in centimeters when the length of a person's femur (thighbone) is known. Find $f^{-1}(x)$ and explain what it computes.