

Name: _____ Period: ____ Date: _____

NON-CALCULATOR SECTION

Vocabulary: Define each word and give an example.

1. radioactive decay
2. common logarithm

Short Answer:

3. Explain how to determine if an exponential function is a growth or decay model.
4. Derive the change of base formula for logarithms.
5. Describe the domain and range of the natural logarithm function.

Review:

6. By the fundamental theorem of algebra, the function $f(x) = x^4 + 3x^3 - 3x^2 + 3x - 4$ has how many complex zeros? _____ Find all of the complex zeros.
7. Write a polynomial function, $f(x)$, with real coefficients in standard form that has zeros -2 and $1 + 2i$.
8. Find the inverse relation of $f(x) = 2\sqrt{x} + 3$.

Problems:

Be sure to show all work used to obtain your answer. Circle or box in the final answer.

9. Determine a formula for an exponential function that passes through the points $(0,2)$ and $(3,1)$.

9. Describe how to transform the graph of $f(x) = -4^{-x}$ into the graph of $g(x) = 2^x$.

10. Find the y-intercept and horizontal asymptotes of $f(x) = \frac{64}{5 + 3e^{-0.05x}}$.

11. Find the exponential function that satisfies the given conditions: Initial value = 24, increasing at a rate of 5.4% per day.

12. Evaluate the following logarithms.

A. $\log_2 32$

B. $\log_5 \frac{1}{25}$

C. $\log 10000$

D. $\ln \frac{1}{\sqrt[3]{e}}$

13. Rewrite the equations in exponential form.

a. $\log_3 x = 4$

b. $\ln \frac{x}{y} = -4$

c. $\log \frac{a}{b} = -2$

14. Solve the equations.

a. $3^{x-3} = 5$

b. $3 \log_2 x + 1 = 7$

c. $\ln(3x+4) - \ln(2x+1) = 5$

15. Use the properties of logarithms to write the expression $3 \log(x+8) - 2 \log(x-5)$ as a single logarithm.

16. Describe the sequence of transformations used to graph the function $y = -\log_2(x+1) + 4$. Then graph the function. Fill in the characteristics of the graph.

Domain: _____

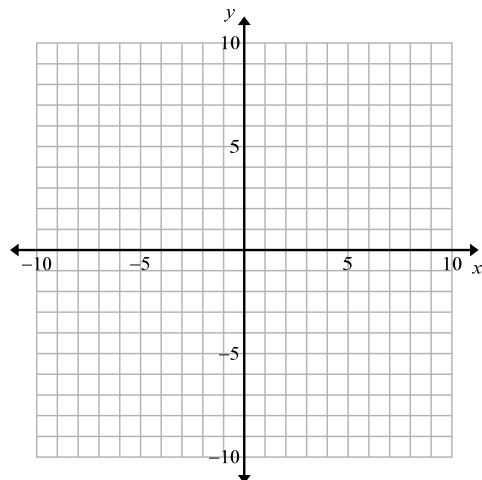
Range: _____

y-intercept(s): _____

x-intercept(s): _____

Asymptotes(s): _____

End Behaviors in Limit Notation: _____



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CALCULATOR SECTION

17. Find the logistic function that satisfies the given conditions: Initial value = 12, limit to growth = 30, passing through (2, 20).

18. Evaluate the following logarithms.

a. $\log_3 13$

b. $\log_5 2$

19. Which expression is equivalent to $\ln \sqrt[5]{\frac{x}{10}}$? (Circle your answer.)

A. $\frac{1}{5} \ln x - \ln 2$

B. $\frac{\ln x}{5 \ln 10}$

C. $\frac{1}{5} \ln x - \frac{1}{5} \ln 10$

D. $\frac{\ln 5}{\ln x - \ln 10}$

E. $\frac{x}{10} \ln 5$

20. A single-cell amoeba doubles every 4 days. How long would it take one amoeba to produce a population of about 10,000 amoebae?

21. Find the amount A accumulated after investing a principal $P = \$4800$ for 17 years at an interest rate 6.2% compounded quarterly.

22. A casserole is removed from a $375^\circ F$ oven, and it cools to $200^\circ F$ after 15 minutes in a $75^\circ F$ room. How long (from the time it is taken out of the oven) does it take to cool to $100^\circ F$? (Use Newton's Law of Cooling: $T(t) = T_m + (T_0 - T_m)e^{-kt}$.)

23. The number P of students infected with flu at ATech t days after exposure is modeled by $P(t) = \frac{300}{1 + e^{4-t}}$.

- What was the initial number of students infected with the flu?
- How many students were infected after 3 days?
- When will 100 students be infected?
- What would be the maximum number of students infected?